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INVESTIGATION OF THE ABSORPTION OF INFRARED RADIATION BY NITROUS OXIDE FROM 760 to 2380 cm⁻¹ (13.2 to 4.2 μm)

by

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ABSTRACT

Experimental data are presented on the absorption by a variety of N_0 samples between 760 and 2380 cm⁻¹. Most of the absorption between 760 and 850 cm⁻¹ is due to extreme wings of lines centered outside the interval. Strengths of the important band systems are given. Curves of transmittance and tables of integrated absorptance and the integrated absorption coefficient provide detailed information on the absorption. The objective of the study is to provide the data required to determine the parameters of all N_0 0 absorption lines that absorb significantly over any atmospheric path of interest.

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INTRODUCTION AND SUMMARY

The work reported herein is part of a large program devoted to the determination and listing of the parameters of all of the spectral lines that absorb significantly in the earth's atmosphere. When completed, the listing will include the parameters such as center position, normalized halfwidth, strength, and the lower energy level for each line. From this information, the molecular absorption can be calculated for virtually any atmospheric path of interest. Nitrous oxide is included in this study, since it is a permanent constituent of the atmosphere. Generally, N_2O lines weaker than 4 x 10^{-23} molecules $^{-1}$ cm 2 cm $^{-1}$ are not considered significant in applications to the earth's atmosphere and will not be included in the listing. A few of the spectral curves shown in this report include lines weaker than this cut-off value because stronger lines in the same region are above the cut-off. The curves may also be useful to workers interested in larger N2O samples than are encountered in atmospheric studies. A few lines weaker than the cut-off value may be included in the listing if they belong to a Q-branch which consists of many closely-spaced lines. In these places, the combination of lines may contribute significantly, although any one of them is very weak.

Measuring the parameters of each individual absorption line would be an impossible task. Many of the lines overlap each other and are too close to be resolved by spectrometers with finite resolving power. The parameters are being determined by a combination of experiment and theory. The strength of a band system is determined experimentally from spectral curves similar to some shown in this report. The band system typically consists of a main band as well as some associated difference bands that arise from transitions from excited energy levels with the same changes in the vibrational quantum numbers as the main band. Corresponding bands of the rare isotopic molecules also overlap the main band. In many cases,

the vibration-rotation interaction does not influence the line strengths significantly and the strength of an individual line can be calculated accurately from the strength of the entire vibration band to which it belongs. The relative strengths of the lines within a band have been tabulated by Young for several types of bands.

The relative strengths of the bands within a system can frequently be estimated on the basis of the relative populations of the lower energy levels involved in the transition. Thus, in many cases, the strengths of the individual lines can be calculated from the experimentally-determined strength of the band system. However, the relative strengths of many of the bands can not be predicted by the simple theory. A considerable portion of the present study has been devoted to investigations of the relative strengths of $\Sigma \leftarrow \Sigma$ bands and their associated difference bands of the $\Pi \leftarrow \Pi$ type. Experimental spectral curves of transmittance are compared with corresponding curves computed on the basis of the calculated line parameters. From these comparisons, it is possible to determine if the calculated strength of a line is too high or too low. This phase of the study has not yet been completed and none of the results are presented in this report.

Sections 2, 3, and 4 include experimental results on absorption by N₂O from 760 to 2380 cm⁻¹. No data are included in the 1350 to 2100 cm⁻¹ region which does not contain any strong bands. The band system that includes the $11^{10} \leftarrow 00^{\circ}0$ band centered near 1880 cm⁻¹ has a strength of 1.66 x 10^{-20} (± 5%) molecules $^{-1}$ cm²cm⁻¹. Several of the lines of this band are strong enough to be included in the listing. Eggers and Crawford² observed a strength of 1.53 x 10^{-20} molecules $^{-1}$ cm²cm⁻¹ for this band system. Their value is approximately 8% less than ours. The $20^{\circ}0 \leftarrow 01^{\circ}0$ band centered near 1974 cm⁻¹ contains a Q-branch whose strength is 2.4×10^{-22} molecules $^{-1}$ cm²cm⁻¹. Further work is planned before the detailed results on the 1350 to 2100 cm⁻¹ region will be reported.

The data presented in Sections 2, 3, and 4 are intended for use in determining the strengths of the various band systems and for comparison with computer data based on the observed band strengths and theory. The data are presented as spectral curves for a variety of samples and as tables of the integrated absorptance and integrated absorption coefficient. The experimental procedures have been discussed previously³. Unless they are indicated otherwise, the positions of band centers and line centers are based on two articles by Pliva⁴, ⁵.

ABSORPTION BETWEEN 760 AND 1100 cm⁻¹

Spectral scans were made throughout the 760 to 850 cm $^{-1}$ region for a variety of large samples of pure N₂O, including one with L = 931 m and p = 1 atm. No structure was observed other than some near 775 cm $^{-1}$ that was attributed to a trace of NO₂ impurity in the N₂O. We concluded that no intrinsic N₂O bands occur in this region with strengths greater than 10⁻²⁴ molecules $^{-1}$ cm $^{-1}$. Near 750 cm $^{-1}$, a few lines were observed and attributed to the wing of the $10^{\circ}O \leftarrow 01^{\circ}O$ system centered near 696 cm $^{-1}$.

Although no line structure was observed, the samples produced significant continuum absorption which may be attributed to the extreme wings of the lines centered outside the interval. The absorption coefficient of the extreme wing of a collision-broadened absorption line increases linearly with pressure, as does the absorber thickness u for a sample cell of fixed length. Thus (- In T) for continuum absorption is proportional to p²L.

By investigating a series of pure N_2O samples covering a range of pressures and path lengths, we determined the normalized absorption coefficient for continuum absorption throughout this spectral region. The results are shown in Fig. 2-1. The transmittance due to continuum for pure N_2O can be calculated from values taken from Fig. 2-1 by:

$$- l_n T = C_s^o up ,$$

where the subscript (s) denotes self-broadening, u is the absorber thickness (in molecules cm⁻²) and p is the pressure in atm. The increase in the coefficient with decreasing wavenumber from the minimum near 830 cm⁻¹ can be explained in terms of the lines of the 696 cm⁻¹ band. The contribution of each line increases as its center is approached. Similarly, the increase between 830 and 850 cm⁻¹ is probably due to the lines in the

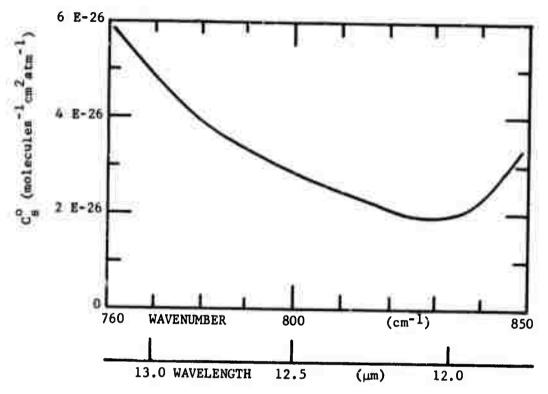
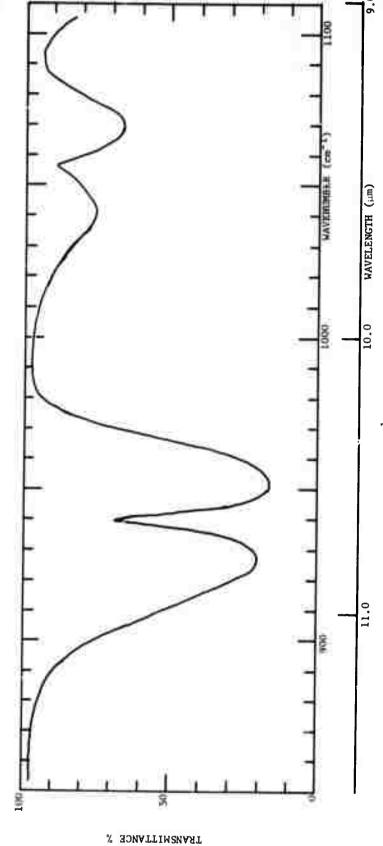


FIG. 2-1. Spectral curve of the normalized absorption coefficient for continuum absorption by pure N_2O at $296^{O}K$.

 $00^{\circ}1 \leftarrow 10^{\circ}0$ band centered near 939 cm⁻¹. In the ordinate of Fig. 2-1 and other similar figures, 2 E-26 denotes 2 x 10^{-26} , etc.

Most of the absorption between 850 and $1100~\rm cm^{-1}$ is due to the two "crossover" bands, $00^{\rm o}1 \leftarrow 02^{\rm o}0$ and $00^{\rm o}1 \leftarrow 10^{\rm o}0$, centered at 1055.622 and 938.849 cm⁻¹, respectively. The associated difference bands arising from transitions from higher excited levels are also present. Figure 2-2 shows a spectral curve of transmittance for a sample at sufficiently high pressure that much of the line structure is smoothed out. The remaining line structure is smoothed by the finite slitwidth of the spectrometer. The P and R branches of the two bands are apparent. Figure 2-3 shows the corresponding spectral curve of (-1/u) $l_{\rm o}$ T. This quantity is nearly independent of u and pressure for pressures sufficiently high that the line structure is smoothed out.



L = 4.16 m; FIG. 2-2. Spectral curve of transmittance from 850 to 1100 cm $^{-1}$. The sample was 3.04 atm of pure N₂O at 296 K. u = 319 x 10²⁰ molecules/cm 2 . Spectral slitwidth is approximately 1.2 cm $^{-1}$.

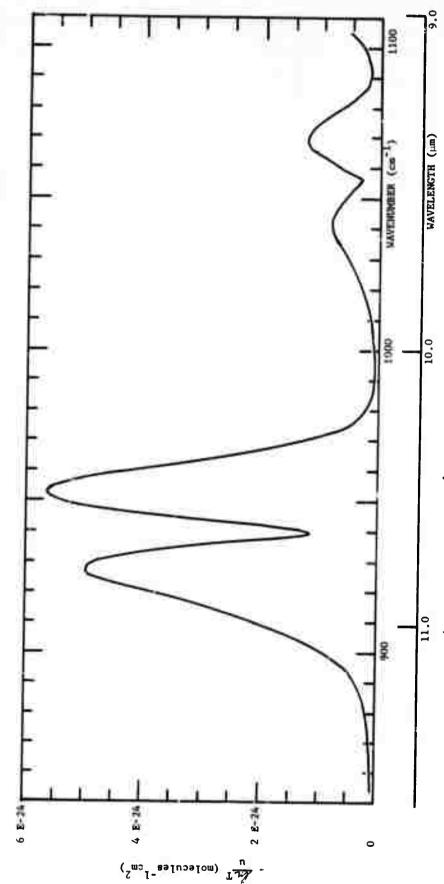


FIG. 2-3. Spectral curve of $(-1/u)_{L^{1}}$ I from 850 to 1100 cm⁻¹. The curve is based on the sample represented in Fig. 2-1.

TABLE 2-1

INTEGRATED ABSORPTION COEFFICIENT BETWEEN 845 AND 1105 cm⁻¹

1	ev	(ln	m\
u	845	(<i>Un</i>	Tyay

	(Multiply all values by	10 ⁻²⁴ molecules 1 cm ² cm	⁻¹)
ν		ι ν	
(cm ⁻¹)		(cm ⁻¹)	
850	3.2	990	2530.1
860	10.1	1000	2537.4
870	18.2	1010	2548.2
880	31.9	1020	2569.1
890	56.1	1030	2610.6
900	114.2	1040	2682.9
910	257.5	1050	2760.9
920	548.3	1056 ^c	2790.9
930	1017.3	1060	2810.3
939 ^c	1311.8	1070	2919.3
			-,-,,,
940	1323.9	1080	3021.9
950	1687.7	1090	3058.€
960	2208.1	1100	3080.1
970	2465.1	1105	3100.8
980	2519.6		5100.0

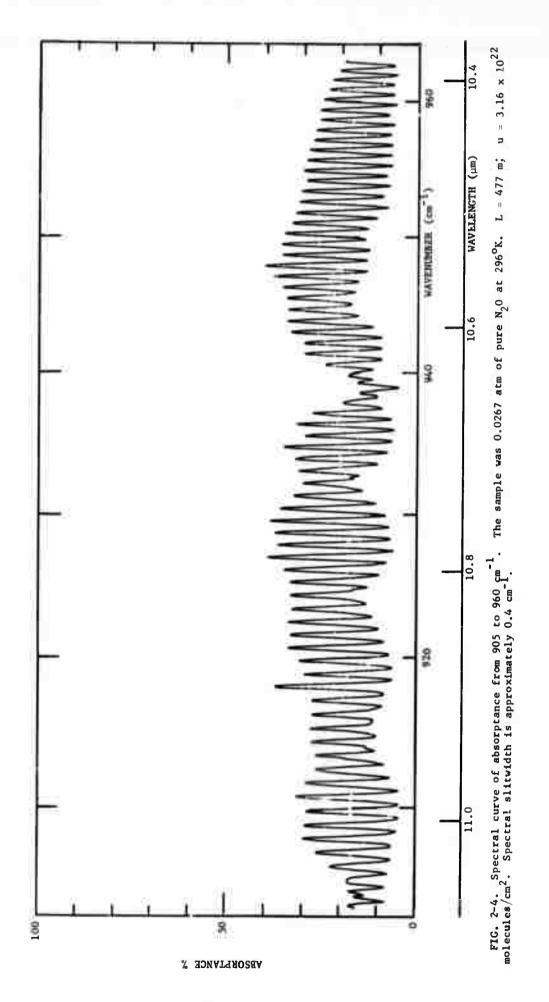
C Denotes position near center of one of the stronger bands.

Table 2-1 gives values of the cumulative integral of the absorption coefficient. The lower limit of integration is 845 cm⁻¹. By assuming that the absorption from 845 to 1000 cm⁻¹ is due to the 00°1 \leftarrow 10°0 band and its associated difference bands, and that from 1000 to 1100 cm⁻¹ is due to the 00°1 \leftarrow 02°0 band and its associated bands, we can determine the strengths of each band system from Table 2-1. The tabulated value of $\int (-1/u) \int_0^u T dv$ at 1000 cm⁻¹ is 2537.4 x 10⁻²⁴ molecules $^{-1}$ cm²cm⁻¹; therefore, the strength of the 00°1 \leftarrow 10°0 band system is approximately 254 x 10⁻²³ molecules $^{-1}$ cm²cm⁻¹. The strength of the 00°1 \leftarrow 02°0 band system is approximately 54 x 10⁻²³ molecules $^{-1}$ cm²cm⁻¹. The estimated uncertainty is \pm 4% for the 00°1 \leftarrow 00°0 system and \pm 8% fpr the weaker 00°1 \leftarrow 02°0 system which is overlapped by the wing of the much stronger 02°0 band centered near 1168 cm⁻¹.

Similarly, we can show from Table 2-1 that 1312/2537 = 51.8% of the strength of the $00^{\circ}1 \leftarrow 10^{\circ}0$ system lies below 939 cm⁻¹, the center of the main band. From theory, we expect approximately 48.8% of the strength of a single $\Sigma \leftarrow \Sigma$ band of a rigid rotator to occur in the P-branch on the low wavenumber side of the center. The additional strength observed in the P-branch can be attributed to the associated difference bands, primarily the $01^{\circ}1 \leftarrow 11^{\circ}10^{$

The lines of the 00°1 \leftarrow 10°0 band are the only ones in this region that are strong enough to meet our criterion for consideration in absorption by the earth's atmosphere. Spectral curves showing much of the line structure in the region of this band are shown in Figs. 2-4 and 2-5. The sample represented in Fig. 2-4 was at sufficiently low pressure and long path that the contribution of the weak lines of the associated difference bands provide a significant portion of the absorption and modify the shape of the spectral curve. The absorptance minimum near the band center at 939 cm⁻¹ is apparent, but an envelope curve connecting the points of maximum absorptance is not smooth as it usually is for a band of this type when the sample pressure is higher. Several unresolved, weak lines of difference bands are intermingled with the main lines and produce the irregular structure. When the pressure is low, the lines are narrow and the maximum amount of absorptance observed with a finite spectral slitwidth depends strongly on the separation between the lines contributing most of the absorption.

Spectral curves in the wings of the band are shown in Fig. 2-5 for a larger sample. The influence of unresolved weak lines is also apparent in these curves, particularly between 850 and 905 cm⁻¹.



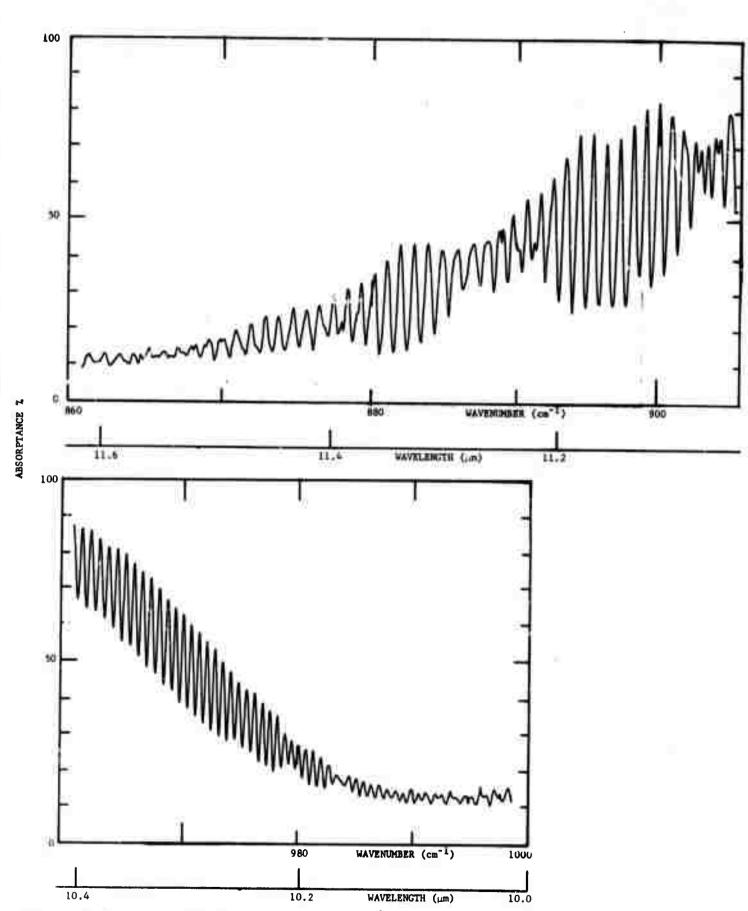


FIG. 2-5. Spectral curve of absorptance from 860 to 905 cm $^{-1}$ and from 961 to 1000 cm $^{-1}$. The sample was 0.20 atm of pure N₂O at 296°K. $t_{\rm c}=477$ m; $t_{\rm c}=2.37 \times 10^{23}$ molecules/cm 2 . Spectral slitwidth is approximately 0.4 cm $^{-1}$.

ABSORPTION BETWEEN 1100 AND 1350 cm⁻¹

Most of the absorption in this region is due to the $02^{\circ}0 \leftarrow 00^{\circ}0$, and $10^{\circ}0 \leftarrow 00^{\circ}0$ bands centered at 1168.134 and 1284.907 cm⁻¹, respectively. The associated difference bands, $03^{\circ}0 \leftarrow 01^{\circ}0$ and $11^{\circ}0 \leftarrow 01^{\circ}0$, are centered at 1160.291 and 1291.501 cm⁻¹, respectively. Figures 3-1 and 3-2 show spectral curves of transmittance for samples at sufficiently high pressure that the line structure is smoothed out. The corresponding curves of $(-1/u) \ln T$ appear in Figs. 3-3 and 3-4.

Values of the cumulative integral $\int_{\nu}^{\nu} (-1/u) \int_{m} T d\nu$ are listed for several values of ν in Table 3-1. From this table, we see that the strength of the $02^{\circ}0 \leftarrow 00^{\circ}0$ band system is 38.5×10^{-20} molecules $^{-1} \text{cm}^{-2} \text{cm}^{-1}$, the value of the integral from $\nu' = 1110$ to $\nu = 1235$ cm $^{-1}$. The strength of the system containing the $10^{\circ}0 \leftarrow 00^{\circ}0$ band is 996×10^{-20} molecules $^{-1} \text{cm}^{-2} \text{cm}^{-1}$. The estimated uncertainty is $\pm 4\%$ for both of these values which compare favorably with the corresponding values 40.5×10^{-20} and 986×10^{-20} molecules $^{-1} \text{cm}^{-2} \text{cm}^{-1}$ reported by Goody and Wormell 6 .

Figures 3-5 to 3-10 show spectral curves of a variety of samples at sufficiently low pressures that much of the line structure is retained. The influence of the difference bands on the spectral curves is apparent. Part of the feature near $1160~\rm cm^{-1}$ is undoubtedly due to the Q-branch of the $03^{1}0 \leftarrow 01^{1}0$ band associated with the $02^{0}0 \leftarrow 00^{0}0$ band; i.e., both bands involve the same changes in vibrational quantum numbers. The feature near $1292~\rm cm^{-1}$ is due to the Q-branch of the $11^{1}0 \leftarrow 01^{1}0$ difference band. Other lines of the difference bands are also apparent in different portions of the spectrum. The curve shown in Fig. 3-7 was obtained with a narrower slitwidth than were the other curves and consequently contains more structure. Different panels in the same figure represent different spectral

regions. The portion between the vertical broken line and the nearest edge of the panel is repeated in the adjacent panel.

Values of the cumulative integral of absorptance are listed in Tables 3-2 and 3-3 for the samples represented in Figs. 3-5 to 3-10. The sample numbers are given in the figures, and the sample parameters are listed in the figure legends.

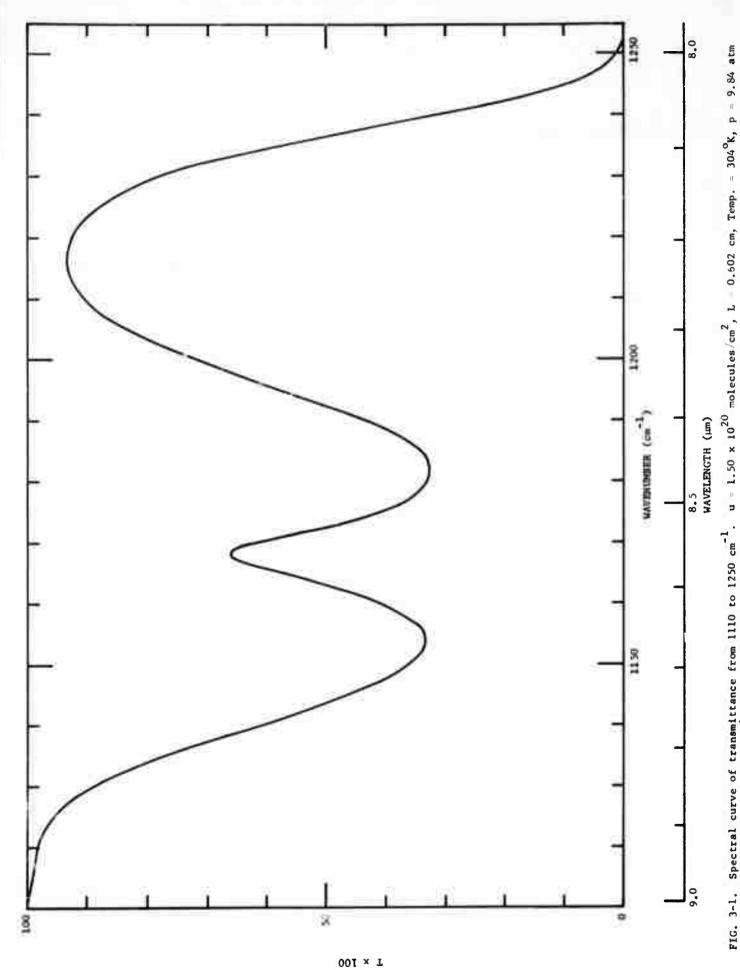


FIG. 3-1. Spectral curve of transmittance from 1110 to 1250 cm $^{-1}$ pure N₂O. Spectral slitwidth ${\rm \framemum}$ 1 cm $^{-1}$.

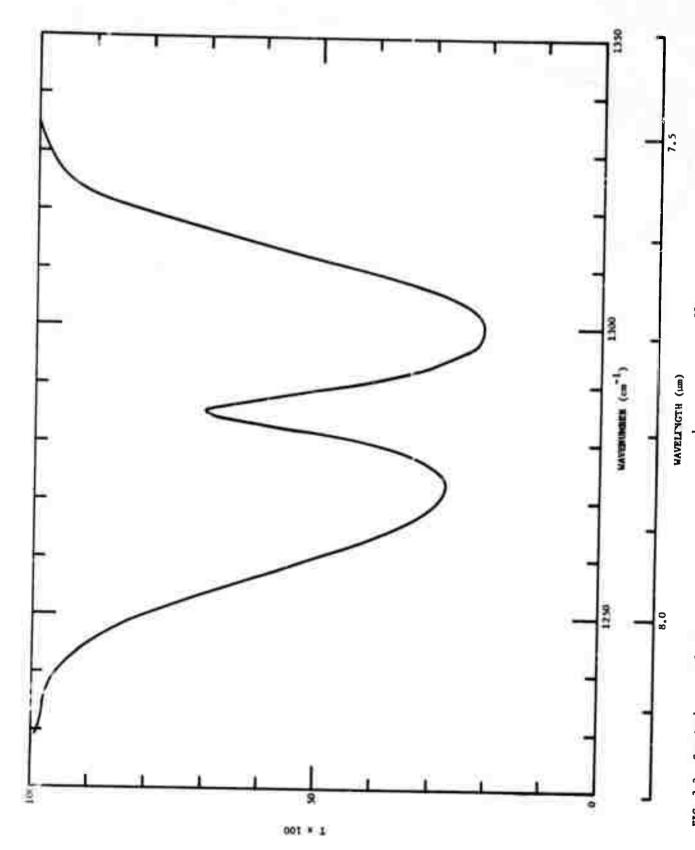


FIG. 3-2. Spectral curve of transmittance from 1220 to 1350 cm⁻¹. $u = 0.0647 \times 16^{20}$ molecules/cm², L = 0.662 cm, Temp. = 302°K p = 0.441 atm with N₂ added to give a total pressure P = 10.59 atm. Spectral slitwidth 0.8 cm⁻¹.

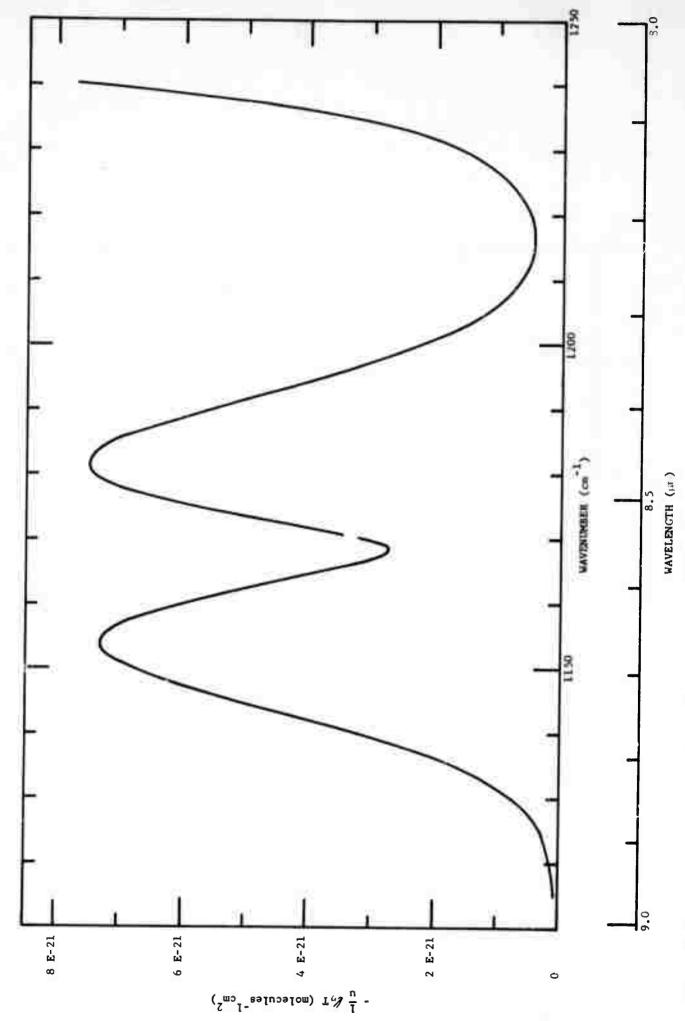


FIG. 3-3. Spectral curve of $(-1/u) \iota^2$. T for N₂O from 1110 to 1250 cm⁻¹.

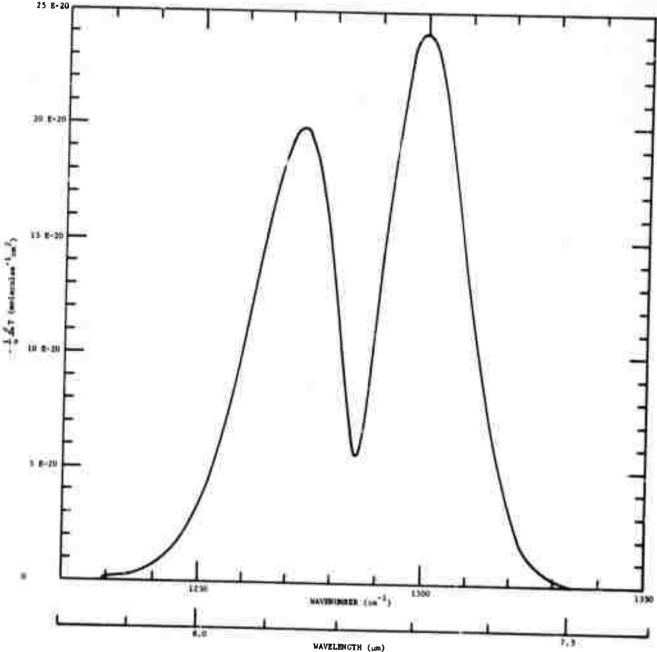


FIG. 3-4. Spectral curve of (-1/u) AT for N20 from 1220 to 1350 cm 1.

TABLE 3-1

INTEGRATED ABSORPTION COEFFICIENT
BETWEEN 1110 and 1335 cm⁻¹

Multiply al	l values	of	the	integral	bу	10-22	molecules	1 cm ² cm ⁻¹

(cm ⁻¹)	$\int_{V'}^{V} \frac{1}{u} (-\mathcal{L}_n T) dv$ $V' = 1110 (cm^{-1})$	(cm ⁻¹)	$\int_{v'}^{v} \frac{1}{u} (-\ln T) dv$ $v' = 1230 (cm^{-1})$
1115	2.464	1240	396.02
1120	7.132	1245	943.17
1125	17.008	1250	2127.17
1130	41.473	1255	4514.95
1135	100.002	1260	8715.40
1140	221.625	1265	15219.14
1145	431.254	1270	23978.49
1150	732.638	1275	33824.89
1155	1090.493	1280	42226.34
1160	1426.870	1285	46726.19
1165	1670.950	1290	50820.09
1170	1823.011	1295	59439.37
1175	2050.138	1300	71060.17
1180	2391.468	1305	82442.49
1185	2761.407	1310	90916.23
1190	3081.160	1315	95872.33
1195	3311.339	1320	98312.92
1200	3457.245	1325	99246.15
1205	3539.731	1330	99539.19
1210	3583.604	1335	99603.51
1215	3610.055		
1220	3633.258		
1225	3665.461		
1230	3724.761		
1235	3845.686		

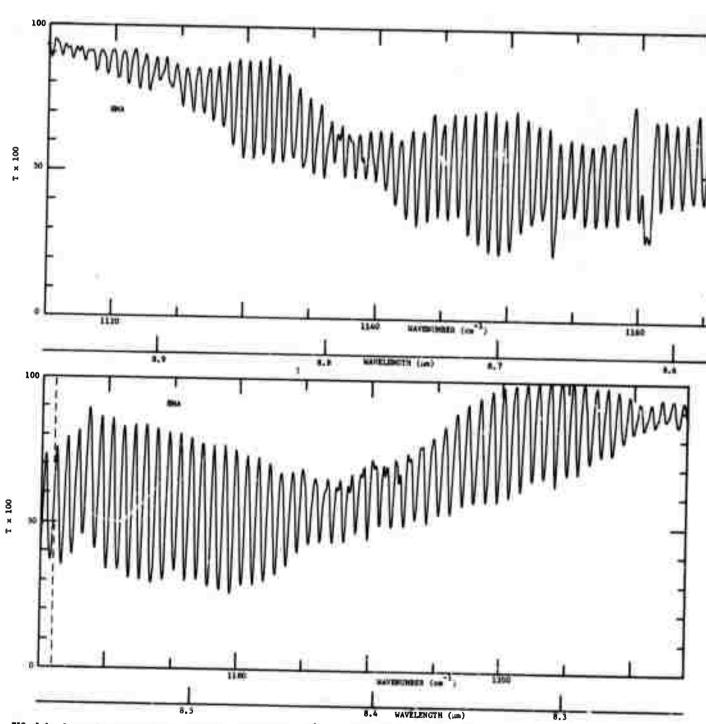


FIG. 3-5. Spectral curve of transmittence from 1115 to 15 cm⁻¹. u = 31.0 x 10²⁰ moleculee/cm², L = 123.4 m, Temp. = 296°K, p = 0.0101 atm

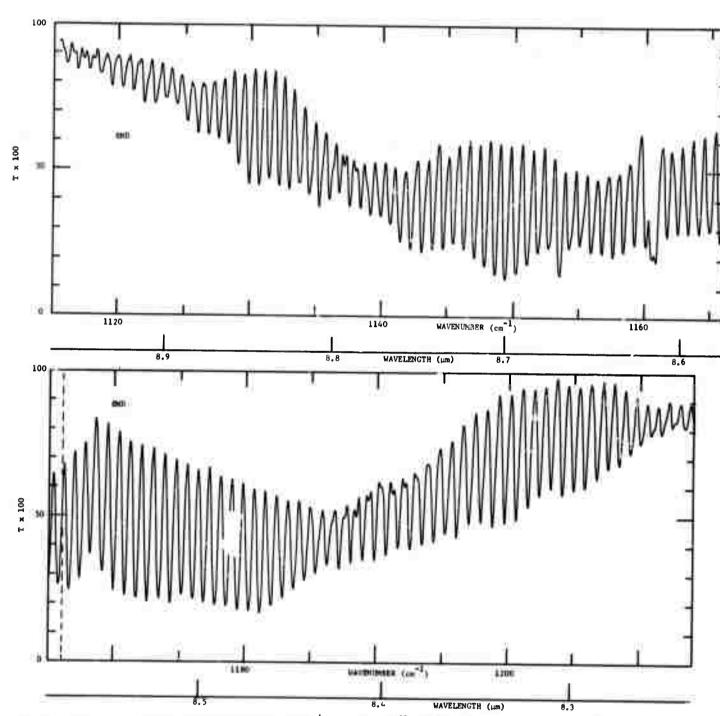


FIG. 3-6. Spectral curve of transmittance from 1115 to 1230 cm⁻¹. u = 41.5 x 10²⁰ molecules/cm², L = 123.4 m, Temp. = 296°K, p = 0.0136 atm pure N₂0. Spectral alitwidth = 0.3 cm⁻¹.

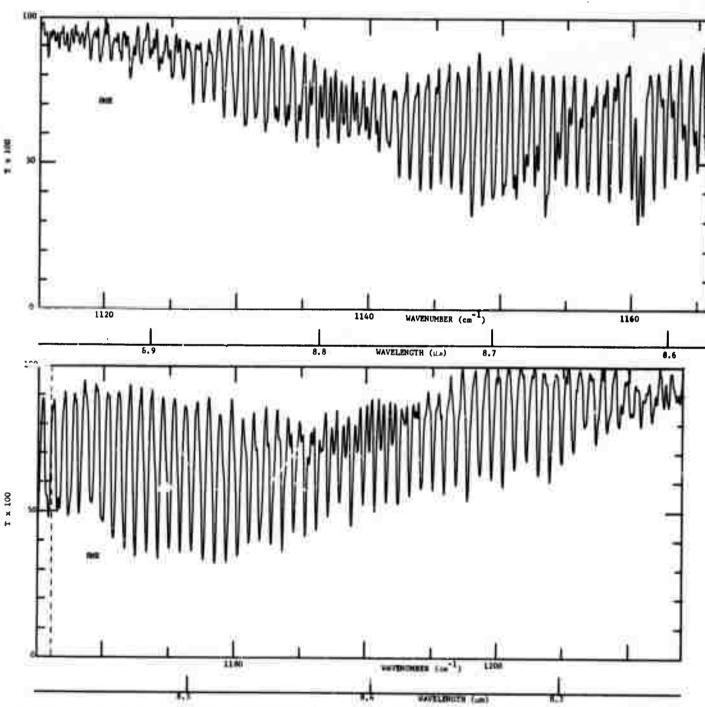


FIG. 3-7. Spectral curve of transmittance from 1115 to 1715 cm⁻¹. u = 20.9 x 10²⁰ molecules/cm², L = 123.4 m, Temp = 296°K, p = 0.0068 etm pure N₂O. Spectral elitwidth # 0.2 cm⁻¹.

TABLE 3-2 $[\int_{v'}^{v} A(v)dv] (v'=1115 \text{ cm}^{-1})$

Sam. No. p (atm) u (#/cm ²)		8MA 0.0101 31.0 E20	8MD 0.0136 41.5 E20	8ME 0.0068 20.9 E20	Sam. No. p (atm) u (#/cm ²)	8MA 0.0101 31.0 E20	8MD 0.0136 41.5 E20	8ME 0.0068 20.9 E20
		1		!				1
ν -1.				·	V _1		1	
(cm ⁻¹)			:		(cm ⁻¹)			
1115		C.	0,	0,	1165	18,621	23,001	43'540
1116	!	0.081	0,093	0.057	1166	19,081	23,567	13,540 13,279
1117		0,173	0,207	0.130	1167	19.491	24,672	14 143
1115		0,270	0,327	0.203	1168	19,874	24,536	14,163 14,435
1119		0,385	0.459	0,233 0,276	1166	20.210	24,543	14.690
1120		0,501	0,603	0;357	1170	20,620	25,437	
1121		0,632	C,751	0,441	1171	21,044	25,940	14,997 15,314 15,605 15,901
1122		0.751	0,544	0,553	11.72	21,441	26,435	15 6 5
1123		0,944	1.144	2.654	11/3	21,634	26,933	15,005
1124		1,093	1,339	0.743	1174	22,267	27,473	16,242
1125		1,272	1,564	0,874	1175	22 754	26 440	
1126		1,485	1.638	1,009	1176	22,751	28,049	16,614
1127		1.710	2,122	1,146	1177	23.227	25,641	16,978
1128		1.925	2,390	1,3,3	1178	23,692	29,215	17,301
1129		2,162	2,686	1,464	1179	24,146	29,78 ₀ 30,346	17,635
1130		2.465	3,056	1,569	4.44			
1131		2,741	3,399	1 845	1180	25,673	30,952	18,343
1132		2,999	3,719	1,845	1181	25.576	31,584	15,735
1133		3,334	4,132	2,264	1162	26,130	32,235	19,130
1134		3,667	4,553	2,524	1183	25,501 27,067	32,654	19,490
1135		4 040	4 054			·		
1136		4,012 4,390	4,966	2,765	1165	27,467	34,012	20,127
1137		4.8:5	5,461 5,972	3,040	1186	27,920	34,583	20,456
1133	r	5,208	6,480	3,354	1187	28,354	35,142	20.761
1137	•	5.636	7,616	3,966	1189	25,793 29,220	35,695	21,067
1440		4 .000				2,1660		21,363
1140		6.092	7,597	4,294	1190	29,611	36: /29	21,653
1141		6,546	8,183	4,524	1191	29,964	37,190	21,894
1142 1143		7,015	6,780	4,952	1192	30.329	77,647	22,145
1144		7,521 8,040	9,400	5,362 5,564	1193	30,683	36,092	22,369
		0,346		3,394	1194	31,014	38,511	22,607
145	*	3,481	10.602	6,035	1195	31,334	38,914	22,329
166		6,923	11,157	6,347	1196	31,645	39,321	23,067
147		9,412	11,769	6,699	1197	31,922	39,686	23,251
.148 149		9,964 10,458	12,428	7,134	1198	32,1EE	40,624	23,435
		10,430	13,536	7,510	1199	32,417	40,336	23,592
150		10,973	13,674	7,975	1200	32,699	40,602	23,724
151		11,520	14,340	6,205	1201	32,779	40,841	23.858
152		12,056	15,000	8,716 9,112	1202	32,937	41,070	23,964
.153 .154		12,572	15,632	9,112	1203	33,092	41,290	24,109
.1.7		13,119	16.280	9,513	1204	33.255	41.506	24,276
155		13,535	16,926	9,900	1205	33,413	41,741	24,433
156		14,172	17,587	10,253	1206	33,554	41,956	24,433
	1	14,699	18,237	10,653	1207	33,683	42,140	24,644
156		15,107	16,647	11.008	1208	33,900	42.295	24,749
159		15,664	19,440	11,342	1209	33,938	42,473	24,551
160		16,122	20,006	11,687	1213	34,074	42.665	24' 97
151		16,783	20,759	12.216	1211	34,193	42.643	24,97.
102		17,216	21.297	12.331	1212	34,300	43,003	25 214
163		17,663	21,846	12,046 13,177	1213	34.393	43,145	25,214
164		15.141	22,415	13,177	1214	34,499	43.292	25,373

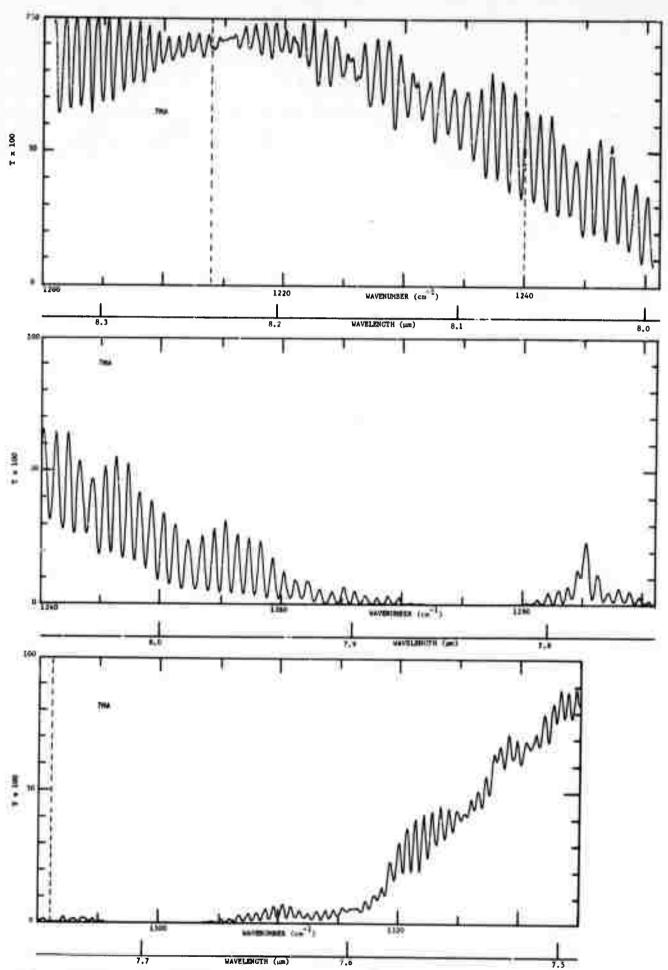
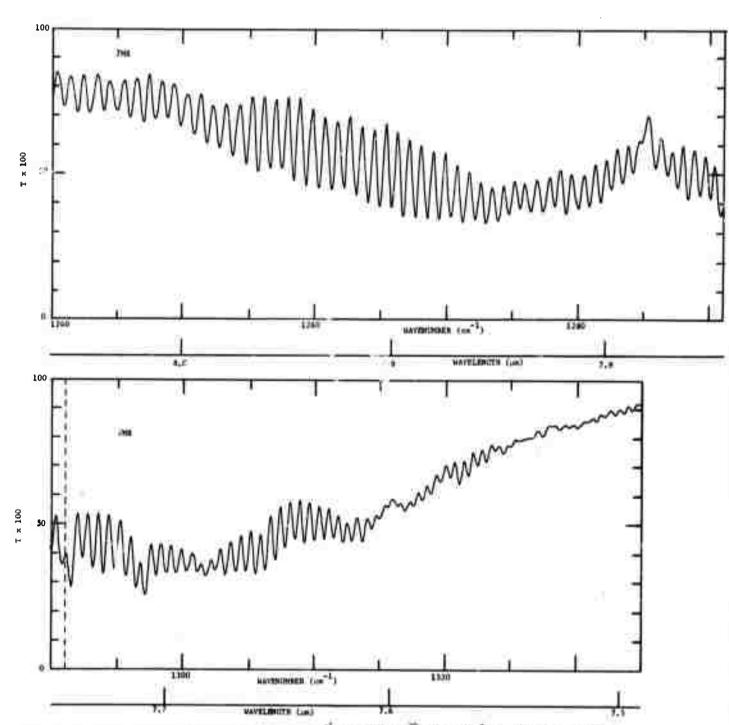


FIG. 3-8. Spectral curve of transmittance from 1200 to 1335 cm⁻¹. $u = 31.0 \times 10^{20}$ molecules/cm², L = 123.4 m, Temp. = 296°K, p = 0.0101 atm pure N₂0. Spectral slitwidth = 0.4 cm⁻¹.



PIG. 3-9. Spectral curva of transmittance from 1240 to 1335 cm p = 0.00126 atm pure N₂0. Spectral alithidth % 0.45 cm⁻¹.

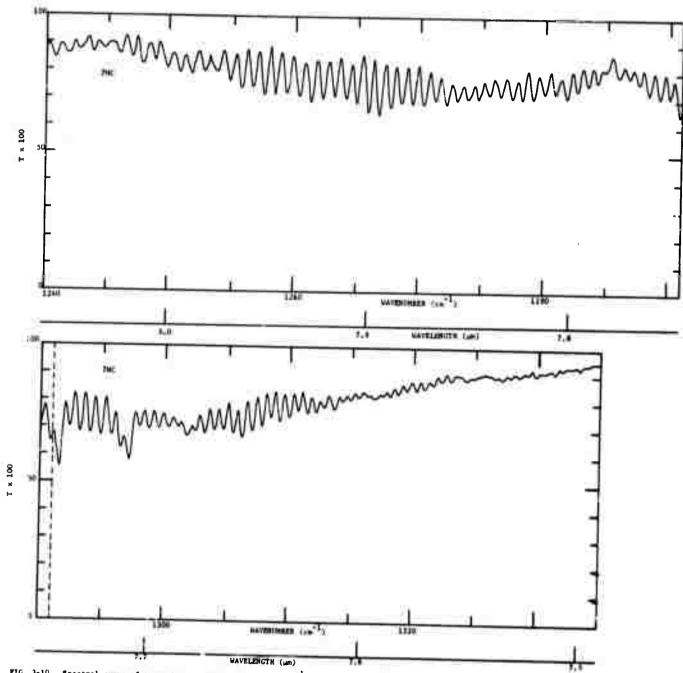


FIG. 3-10. Spectral curve of transmittance from 1240 to 1335 cm⁻¹. $u=4.98 \times 10^{20}$ molaculas/cm², L=477 m, Temp. = 296°K, p = 3-14

TABLE 3-3 $\{\int_{v^{+}}^{v} A(v) dv\} \ (v^{+}=1240 \text{ cm}^{-1})$

p (atm) u (#/cm²)	0.0101 31.0 E20	0.00126 14.9 E20	0.00042 4.98 E20	Sam. No. p (atm) u (#/cm ²)	7MA 0.0101 31.0 E20	7MB 0.00126 14.9 E20	7MC 0.00042 4.98 E2
	1			- (1/5111)	J1.0 E20	1 .4.7 E20	7.70 EZ
v -1		į.	!	ν,		1	
(cm ⁻¹)	1			(cm ⁻¹)		•	1
40	0	0:	0.	1295	48,961	24,016	11,746
41	0.519	0,209	0,134	1296	49,957	24.593	12,069
42	1,068	0,433	0.362	1297	50,954	25,252	12.349
43	1,624	0.663	0.381	1298	51,954	25,905	12,666
144	2,228	c.885	0.491	1299	52,954	26,525	12,941
45	2,885	1,119	0.604	1300	53,954	27,142	13.209
46	3,527	1,355	0,723	1301	54,954	27,770	13,467
47	4,170	1,596	0,839	1302	55,954	25,426	13,769
43	4,829	1,838	0,973	1303	56,954	29,050	14,078
149	5,553	2.050	1,104	1304	57,952	27,672	14.359
59	6,339	2.339	1,258	1305	58,946	30.276	14,627
5:	7,101	2.629	1,429	1306	59,934	30,860	14,890
52	7,932	2,937	1.658	1307	60,916	31,435	15,163
53	8.782	3,271	1,777	1308	61.894	31,958	15,411
24	9,624	3,620	1,959	1309	62.860	32,430	15,614
55	10,473	3,971	2,142	1310	63,824	32,931	15,840
56	11,305	4,317	2,338	1311	64,776	33.427	16,049
57	12,162	4,668	2,528	1312	65.739	33,924	16,254
58	13,630	5,025	2.732	1313	66,713	34,458	16,469
59	15,905	5,404	2,933	1314	67,674	34,968	16,670
60	14.315	5,806	3,149	1315	68,639	35,456	16,857
51	15,75)	6,239	3,381	1316	69,594	35,892	17,031
62	15,693	6,677	3,613	1317	70,529	36,326	17,210
63	17,643	7,117	3,843	1316	71,445	36,746	17,362
64	15,615	7,592	4,073	1319	72.327	37,136	17,544
55 .	19,586	8,076	4,320	1320	73,101	37,470	17,685
66	20,555	8,550	4,562	1321	73,837	37,785	17.826
67	21,531	9,045	4,819	1322	74,524	35,991	17,952
68	22,515	9,554	5,065	1323	75.189	35,358	16,064
64	23,502	10.078	5,3,1	1324	75.815	39,599	10,167
70	24,485	10,613	5,558	1325	75,419	38,035	18,278
71	25,482	11.174	5,819	1326	75,990	39,045	18,375
72	26,479	11,755	6.069	1327	77.518	39,240	18,478
73	27,479	12,356	6,306	1328	77,946	39,415	18,551
74	29,479	12,569	6,641	1329	78.299	39,575	18,576
75	29,479	13,559	6,908	1330	75,650	39,734	18,765
76	30,479	14,124	7,160	1331	75,984	39,880	19,850
77	31,477	14,699	7,410	1332	79,253	40.010	18,925
78	32,479	15,272	7,669	1333	79,504	40,123	18,995
79	33.479	15,631	7,918	1334	79.67C	46.224	19,058
30 .	34,479	16,402	8,170	1335	79,839	40,312	19,109
1	35,473	16,960	8,407	1336	79,977	40,389	19,157
	36,455	17.489	8,657	1337	81,112	40,468	19,201
3	37,429	17,974	8,576	1338	ep, 193	40,522	19,240
34	35,369	18,437	P. C84	1339	80.287	40,582	19,261
5	39,297	18,858	9;265	1340	80,364	40,639	19,320
6	40,164	19,237	9,457	2341	#0,432	40,687	19,351
7	41,103	19,077	7,653	1342	80,451	40.721	19,368
8	42,068	20,145	7,857	1343	80,462	40,753	19,300
9	43,032	20,638	10,095	1344	60,466	40,778	19,368
0	44,010	21,153	10,345	1345	80.466	40.797	19:388
71	45,001	21.714	18.628		1111,412	****	2.1000
2	45,996	22,331	10,976				
3 .	45,963	22,847					

ABSORPTION BETWEEN 2100 AND 2380 cm⁻¹

Figure 4-1 shows spectral curves of transmittance between 2100 and 2380 cm for a variety of high-pressure samples with the line structure smoothed out. The sample parameters are listed in Table 4-1. The center of the main band, $00^{\circ}1 \leftarrow 00^{\circ}0$, at 2223.756 cm is apparent, and the transmittance maximum near 2322 cm is probably due to the center of the $04^{\circ}0 \leftarrow 00^{\circ}0$ band. All of the obvious features of other bands are smoothed out because of the high sample pressures.

A spectral plot of the absorption coefficient is shown in Fig. 4-2. This plot does not extend below 2140 cm⁻¹ nor above 2270 cm⁻¹ although absorption was observed in these regions. A large portion of the absorption beyond these limits is due to the extreme wings of the very strong lines centered between 2150 and 2250 cm⁻¹. As discussed in Section 2, the continuum absorption coefficient for wing absorption increases linearly with pressure. Thus, the values of $(-1/u) \mathcal{L}_n$ T observed beyond these limits increase with increasing pressure and do not represent the intrinsic absorption due to local lines. By investigating several samples covering a wide range of pressures, we were able to account for the wing absorption and to determine the combined strength of the 2223.756 cm⁻¹ band and its associated difference band. Our value is 5.71 (\pm 0.25) x 10⁻¹⁷ molecules⁻¹cm²cm⁻¹.

Transmittance curves are shown in Figs. 4-3 and 4-4 for three samples at relatively low pressures so that the line structure is retained. The influence of the difference bands on the curves is apparent. The curves in Fig. 4-5 correspond to a sample at very low pressures so that the contributions by the weak lines are much greater relative to that by the strong lines than is the case at higher pressures. Note that the smooth contour such as that observed in Fig. 4-1 is completely modified, even for the curve obtained with wide slits. The transmittance maximum near the center of the

main band, $00^{\circ}1 \leftarrow 00^{\circ}0$ is nearly obliterated, and the Q-branch of the $01^{1}1 \leftarrow 01^{1}0$ band near 2209 is very prominent. There is also evidence of the Q-branch of the $02^{\circ}1 \leftarrow 02^{\circ}0$ and $02^{2}1 \leftarrow 02^{2}0$ bands, both of which are centered near 2195 cm⁻¹.

Values of the integrated absorptance are shown in Table 4-3 for the three samples whose transmittence curves are shown in Figs. 4-3 and 4-4. The sample parameters are listed in Table 4-1. Table 4-2 gives (-1/u) In Table 4-1 for the spectral region from 2145 to 2280.

The absorption at 2290 cm⁻¹ for samples at high pressure is primarily due to the wings of the strong lines of the $00^{\circ}1 \leftarrow 00^{\circ}0$ band centered between 2230 to 2260 cm⁻¹. From the transmittance curves shown in Fig. 4-1 for Samples 4M41 and 4M40, we determined the continuum absorption coefficient at 2290 cm⁻¹ due to the wings of the lines:

$$C_s^0 = 7.55 \times 10^{-23} \text{ molecules}^{-1} \text{cm}^2 \text{atm}^{-1}$$
.

Using the Lorentz line shape, we calculated the absorption coefficient due to the wings of all of the lines of the ν_3 band. The calculated value,

$$C_s^o$$
 (calc) = 39.5 x 10⁻²³ molecules⁻¹ cm² atm⁻¹,

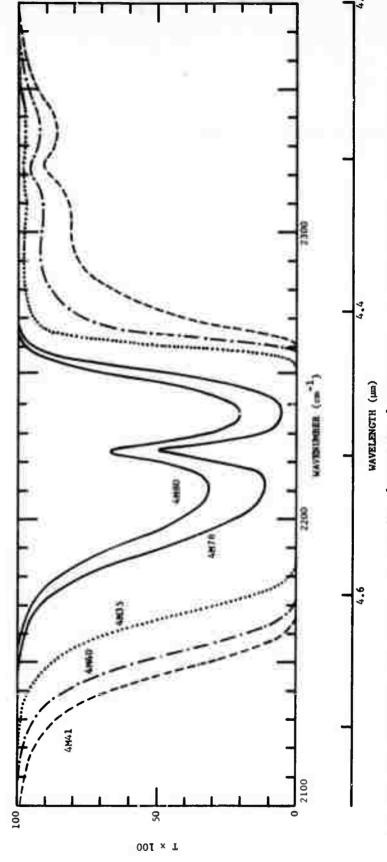
is much larger than the observed value, indicating that the wings of the lines absorb less than the Lorentz line shape predicts.

We also calculated the continuum absorption coefficient by assuming that the shape of the wings of the lines was the same as that determined previously in our laboratory for self-broadened lines of the ν_3 band of CO₂. This value,

$$C_s^o = 5.54 \times 10^{-23} \text{ molecules}^{-1} \text{ cm}^2 \text{ atm}^{-1}$$
,

agrees much better with experiment than does the calculated value based on the Lorentz shape.

Experimental values of the continuum absorption coefficient at 990 cm $^{-1}$ and 1215 cm $^{-1}$ were also considerably smaller than the calculated values based on the Lorentz shape. The continuum at these two points is due primarily to the wings of the $00^{\rm ol}$ \leftarrow $10^{\rm ol}$ and $10^{\rm ol}$ \leftarrow $00^{\rm ol}$ bands, respectively. We conclude that the wings of self-broadened N₂O lines are quite sub-Lorentzian and may be similar in shape to self-broadened CO₂ lines.



The FIG. 4-1. Spectral curve of trensmittance from 2100 cm⁻¹ to 2380 cm⁻¹ for acveral amples at pressures greater than 7 etm. parameters for each sample are given in Table 4-1. Spectral slitwidth = 0.3 cm⁻¹.

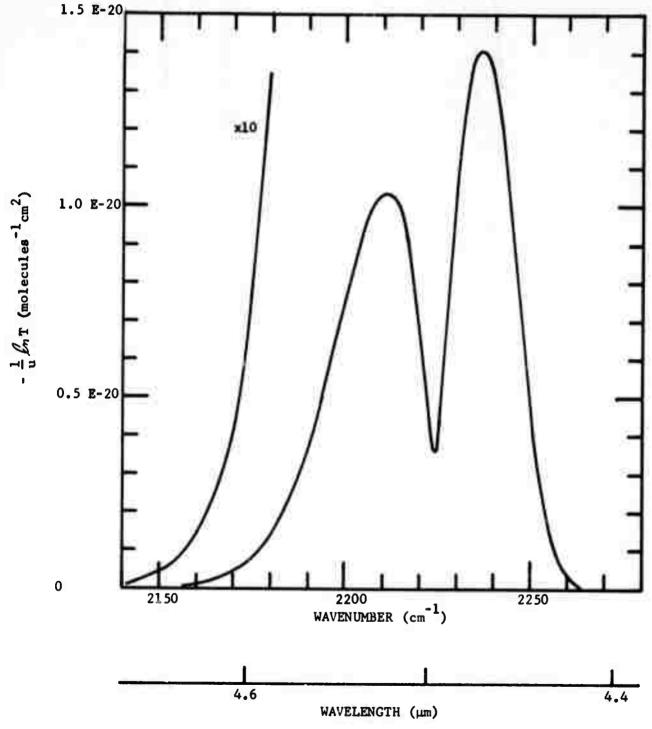


TABLE 4-1

SAMPLE PARAMETERS

Sample Number	P atm	$^{\mathrm{P}_{\mathrm{N}_2}}$	atm	$_{ m molecules/cm}^2$	$\rm s/cm^2$	Temperature oK	L Meters
4M35 4M40 4M41	13.59 7.80 13.59	11.55 0 0	2.04 7.80 13.59	30.1 118.6 212.3	E18 E18 E18	302 302 302	0.00602 0.00602 0.00602
4M48 4M49 4M57	0.1250 0.0625 0.257	000	0.1250 0.0625 0.257	1.845 0.922 3.77	E18 E18 E18	300 300 301	0.00602 0.00602 0.00602
4M78 4M80	8.03 9.03	7.23	0.803	2.00	E18 E18	301 302	0.00102
4МD	0.000087	0	0.000087	128.0	E13	296	595

TABLE 4-2

INTEGRATED ABSORPTION COEFFICIENT BETWEEN 2145 and 2280 cm⁻¹

Multiply all values of the integral by 10⁻²⁰ molecules cm²cm⁻¹

ν	$\int_{0}^{V} \frac{1}{u} (- \int_{0}^{L} T) dt$
(cm ⁻¹)	$v' = 2140 \text{ cm}^{-1}$
2145	0.534
2150	2.161
2155	4.976
2160	10.513
2165	19.137
2170	34.601
2175	61.879
2180	112.003
2185	199.500
2190	345.034
2195	566.959
2200	886.547
2205	1311.890
2210	1808.910
2215	2321.279
2220	2740.897
2225	2965.134
2230	3324.176
2235	3940.207
2240	4634.130
2245	5188.588
2250	5526.007
2255	5662.765
2260	5700.722
2265	5707.949
2270	5709.411
2275	5710.132
2280	5710.187

TABLE 4-3 $[\int_{v'}^{v} A(v) dv] (v'=2162 cm^{-1})$

Sam. No. p (atm) u (#/cm²)	4M57 0.257 3.77 E18	4M48 0.125 1.845 E18	4M49 0.0625 0.922 El8	Sam. No. p (atm) u (#/cm ²)	4M57 0.257 3.77 E 18	4M48 0.125 1.845 E18	4M49 0.0625 0.922 E1
v	i	•					
(cm ⁻¹)		1		V -1.			
(cm)				(cm ⁻¹)			
8105	Ο,	0,	0	2212	18,933	10,215	' K' A & 'R
2163	0,067	0,027	0,017	2213	19,621	13,602	5,453 5,658
2164	0,135	0,057	0,037	2214	20,311	10,987	5,859
2165	0.200	0,085	0,054	2215	27,997	11,364	6,113
2166	0.279	6.124	0.074	2216	21,652	11,781	6.325
2157	9,382	6.171	0,100	2217	22 202	40 444	4'5.4
2166	0,498	0,228	0,131	2218	22,290	12,146	6,536
169	0.627	0,291	0,167	2219	22,950	12,520	6,743
217C	0.760	0,357	0,202	2220	23,619	12,596	6.038
?17 <u>1</u>	0,992	0.414	0.235	2221	24,955	13,260	7,132
4.70					641.722	13,377	7:300
2172	1,050	0,484	0,277	2222	25,364	13,863	7,152
2173 2174	1,221	0,566	0,324	2223	25,377	14,151	7,627
174 ! 175	1,495	0,648	0,370	7224	25,244	14,332	7,726
176	1,509	C,743	0,423	2225	25,734	14,597	7,868
7,0	1,819	0.845	0.476	2226	27,232	14,869	8,019
177	2,047	0,957	0,530	2227	27,774	15,175	
178	2,252	1,063	0,561	2226			8,155
179	2,481	1,163	0,649	2229	29,435	15,566	8,405
180	2,720	1,316	0,721	2236	29.797	15,963	8,514
151	3,002	1,463	0.802	2231	30,457	16,739	9,031
182	3,334	1,642	0,900				
183	3,675	1,817	0,997	2232	31,240	17,108	9,270
164	4.034	1,998	1,097	2233	31,978	17,664	9,462
185	4,394	2,188	1,195	2234 2235	32,695	18,937	9,724
166	4,768	2,381	1,296	2236	33,454	16,479	9,762
187	5,162	2,587					
168	5,564	2,613	1,406	2237	34,939	19,332	10,416
189	6,017	3,041	1,524	2238	35,663	25,749	10,633
190	6,470	3,297	1,642	2239	35,406	20,146	10,840
191	6,917	3,551	1,916	2240	37,139	20,574	11,656
				2241	37,830	20,944	11,249
192	7,306	3,763	2,537	2242	39,548	21,351	11,468
93	7,737	3,999	2,177	2243	39,201	21,488	11,631
194	8,216	4,271	2,325	2244	39.261	22,364	11,432
195	8,734	4,559	2,452	2245	40,494	22,378	11,967
196	9,296	4,873	2,645	2246	41,101	22.700	12,154
97	9,876	5,178	2,814	2247	41,667	23' 044	
98	10,463	5,504	2.990		42,205	23,010	12,314 12,442 12,545
99	11,063	5,840	2,990 3,171	2248 2249	42,723	23,247	12,942
200	11,649	6,180	3,358	2250	43.207	23,539 23,786	12,709
201	12,192	6,492	3,538	2251	43,623	23,991	12,812
102	12,723	6,772	3,688	2050			
203	13.260	7,102	3,864	2252	44,017	24,162	12,90A 12,997
204	13,905	7,455	4,059	2253 2254	44,361	24,360	12,997
05	14,547	7,615	4,242	2255	44,706	24,521	13,000
206	15,197	8,169	4,430	2256	45,225	24,552	13,148
07	15,853	8,534	ì				
08	16,479	8,888	4,620	2257	45,423	24,657	13,256
09	17,082	9,209	4,799	2258 .	45,578	24,930	13.254
10	17,701	9,552	4,970 5,152	2259	45,693	24,986	13,326
	18,333		~ 4 4 4 5	2260	45,790	25,030	13,350

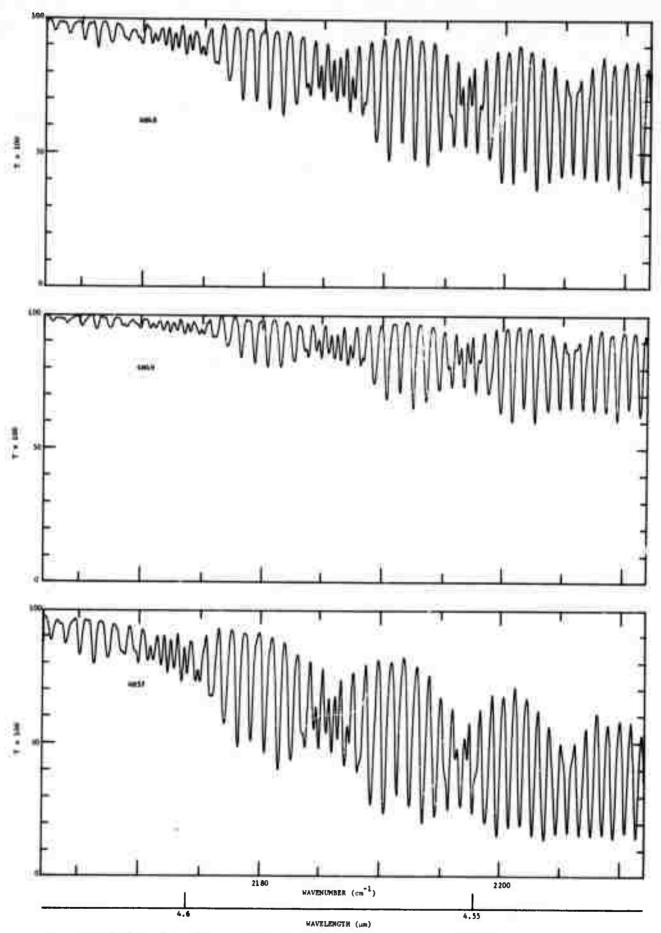


FIG. 4-3. Spectrel curves of trensmittance between 2165 and 2210 cm⁻¹. The eample persmeters are given in Table 4-1. Spectral slitwidth \(\tilde{V} \) 0.3 cm⁻¹.

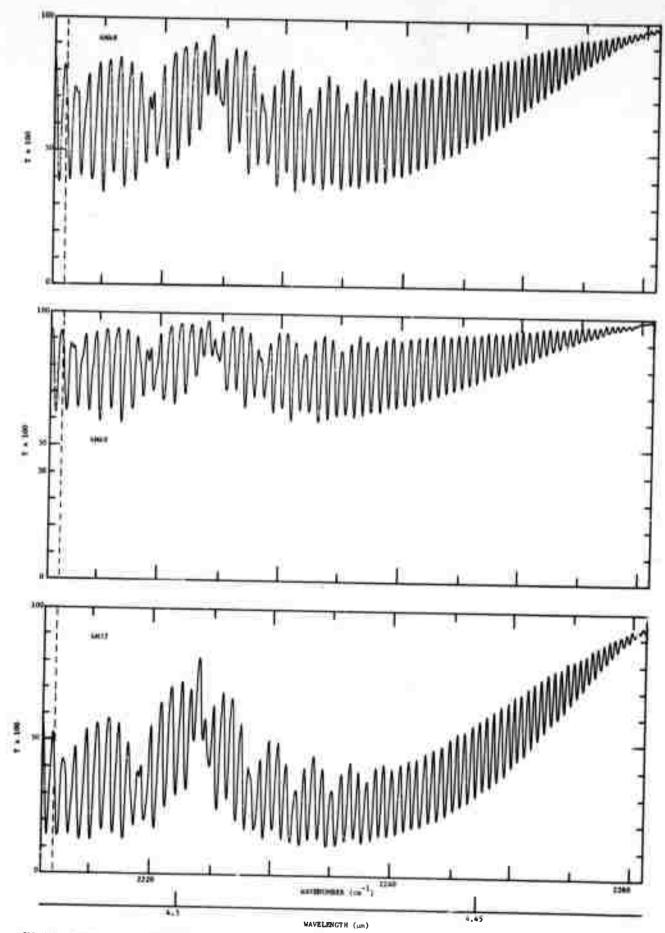


FIG. 4-4. Spectral curves of transmittance between 2210 and 2260 cm⁻¹. The sample parameters are given in Table 4-1.

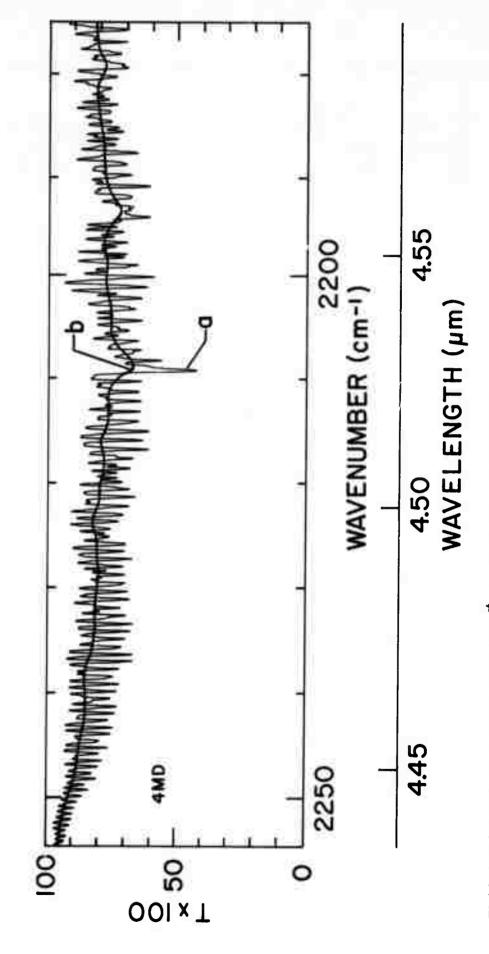


Fig. 4-5. Spectral curves of transmittance for a sample at 0.97 x 10^{-6} cm. Both curves represent the same sample of pure \mathbb{R}_2^0 . Spectral elitridith T 0.2 m^{-1} for curve a and 2.2 m^{-1} for curve b.

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